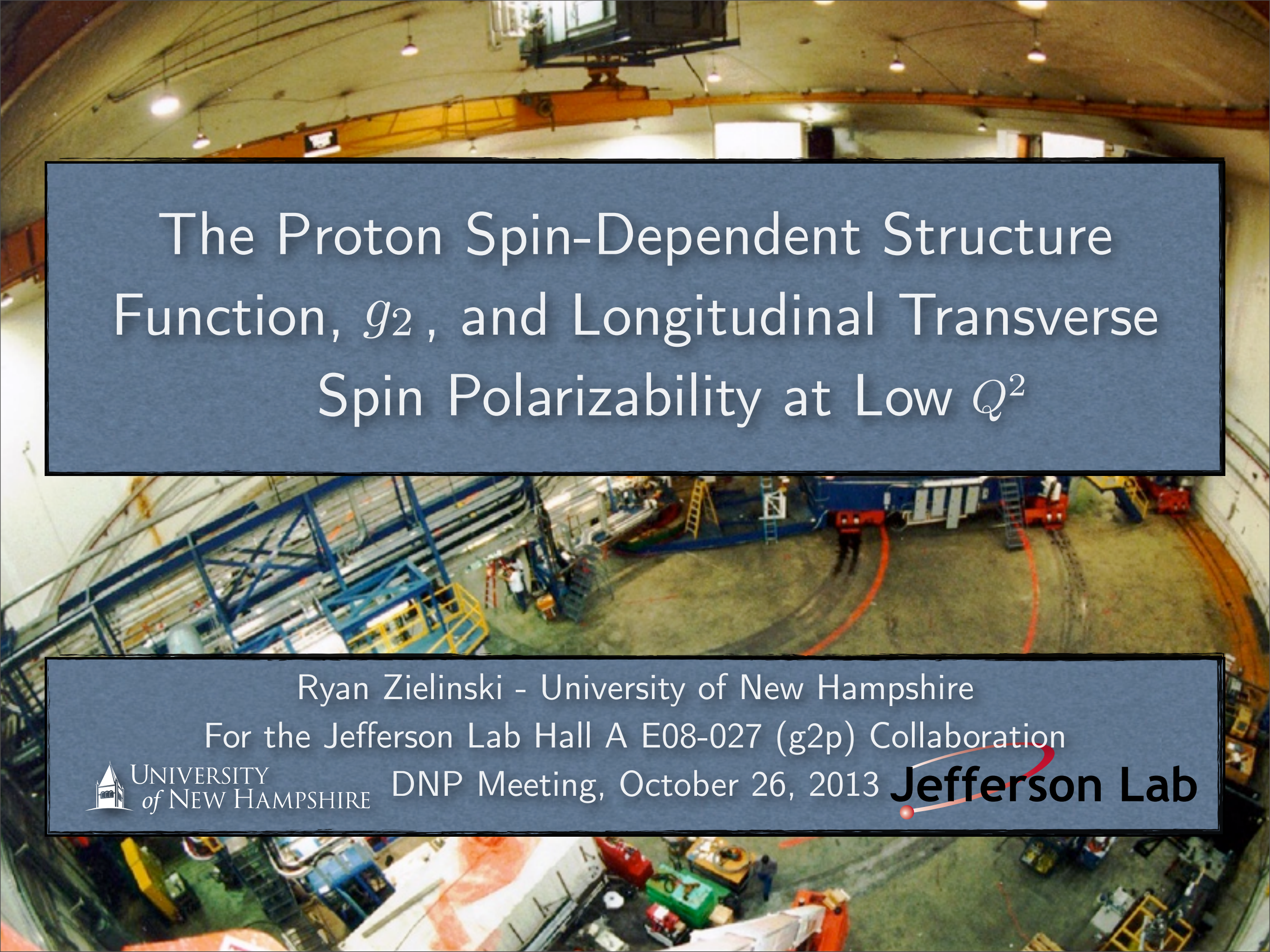




# The Proton Spin-Dependent Structure Function, $g_2$ , and Longitudinal Transverse Spin Polarizability at Low $Q^2$

Ryan Zielinski - University of New Hampshire

For the Jefferson Lab Hall A E08-027 (g2p) Collaboration



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of NEW HAMPSHIRE

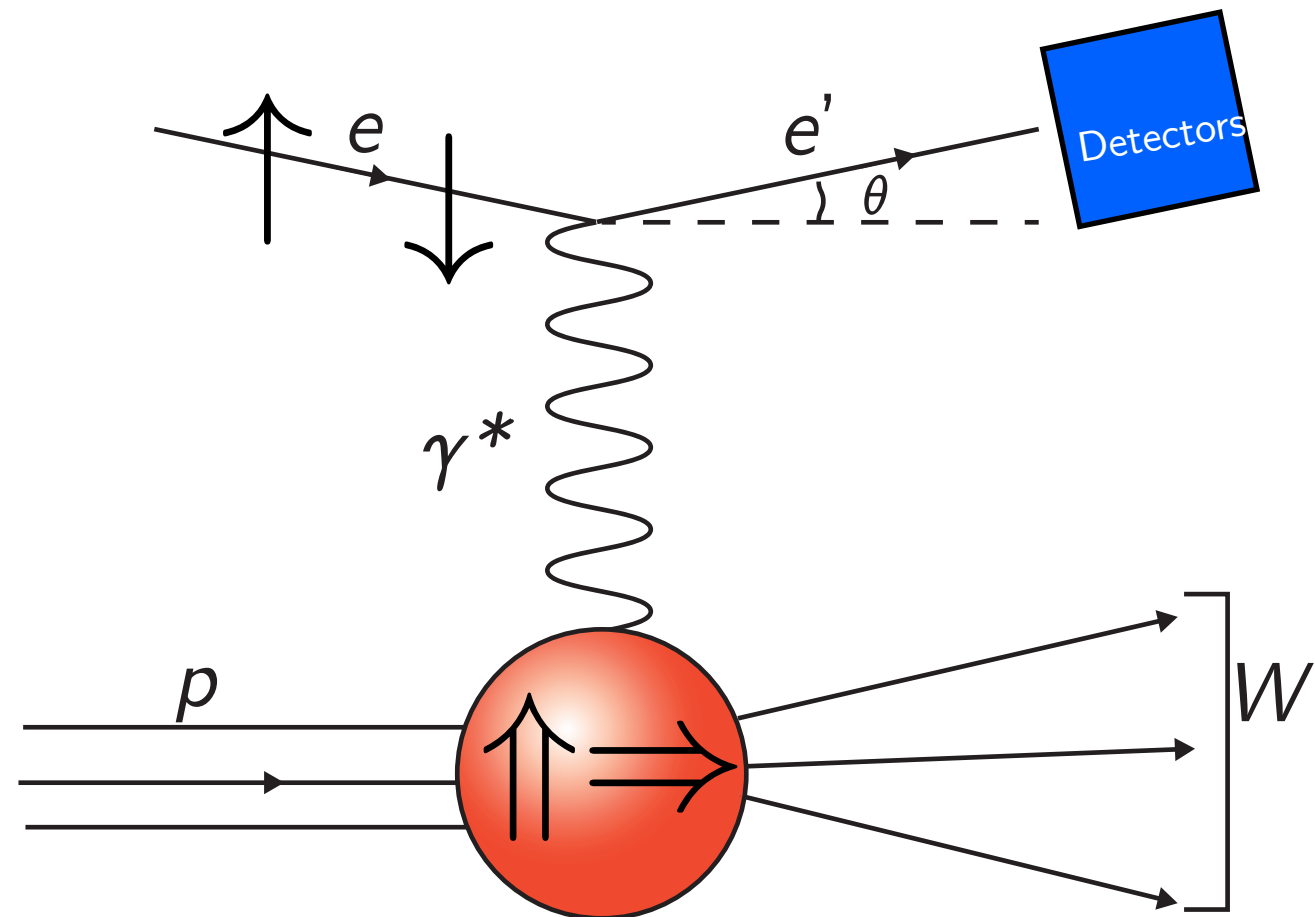
DNP Meeting, October 26, 2013

 **Jefferson Lab**

# Polarized

# Inclusive $ep$ Scattering

- $Q^2$ : 4-momentum transfer
- $W$ : invariant mass of target
- $x$ : momentum fraction
- $\nu$ :  $E - E'$ , energy transfer
- Scattering angle:  $\theta \sim 6^\circ$

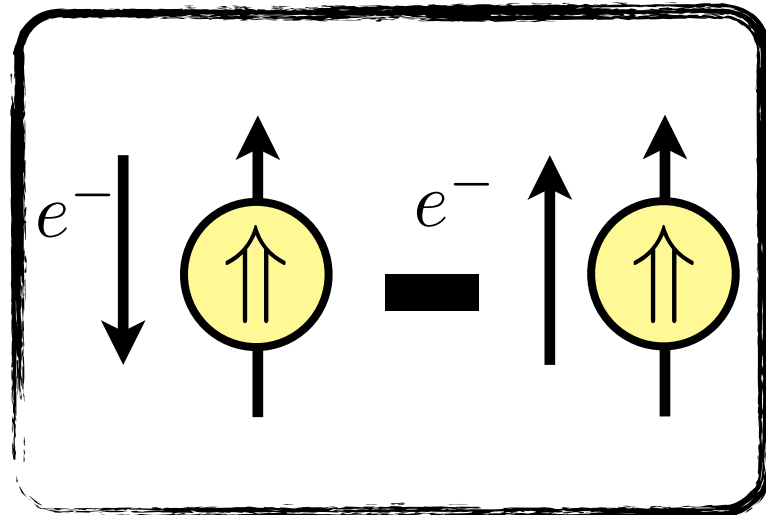


## Spin distribution

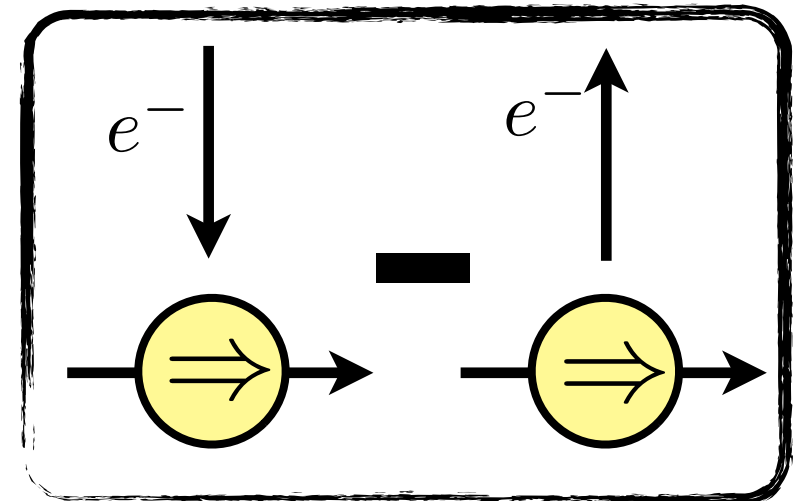
$$\frac{d^2\sigma^\pm}{d\Omega dE'} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} (\alpha F_1(x, Q^2) + \beta F_2(x, Q^2) \pm \gamma g_1(x, Q^2) \pm \delta g_2(x, Q^2))$$

# Extracting Spin Structure

$\Delta\sigma_{\parallel}$



$\Delta\sigma_{\perp}$



- Experiment measured  $\Delta\sigma_{\perp}$  **essential contribution to  $g_2$  in this kinematic region**

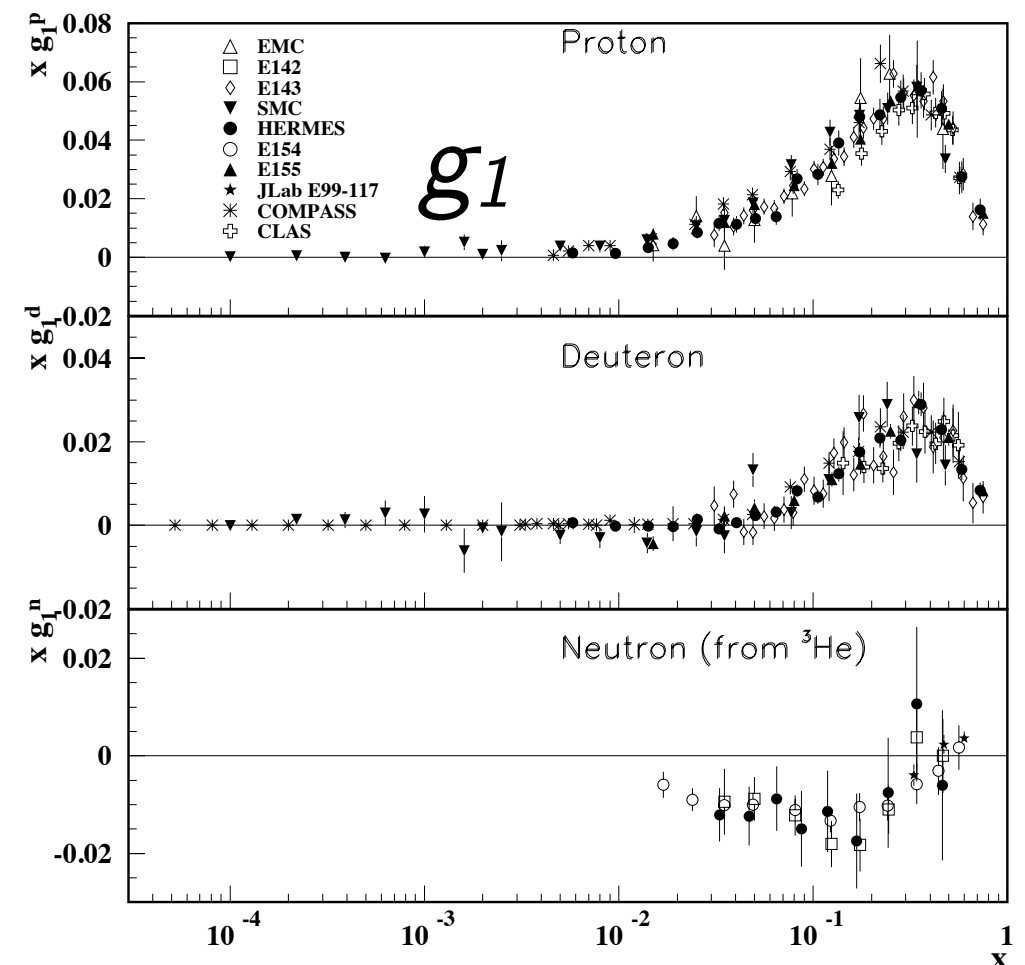
$$g_2^p = \frac{MQ^2}{4\alpha^2} \frac{y^2}{2(1-y)(2-y)} \left( -\Delta\sigma_{\parallel} + \frac{1+(1-y)\cos\theta}{(1-y)\sin\theta} \Delta\sigma_{\perp} \right)$$

- Will use JLab Hall B EG4 data for  $\Delta\sigma_{\parallel}$ .
- Measured  $\Delta\sigma_{\parallel}$  at one kinematic setting as cross-check

# Motivation

Measure a fundamental spin observable ( $g_2^p$ ) in the region  $0.02 < Q^2 < 0.20 \text{ GeV}^2$  for the first time

- Extract  $\delta_{LT}$  as a test of  $\chi$ PT calculations
- Test Burkhardt-Cottingham (BC) sum rule
- Crucial inputs for hydrogen hyperfine splitting and proton charge radius measurements

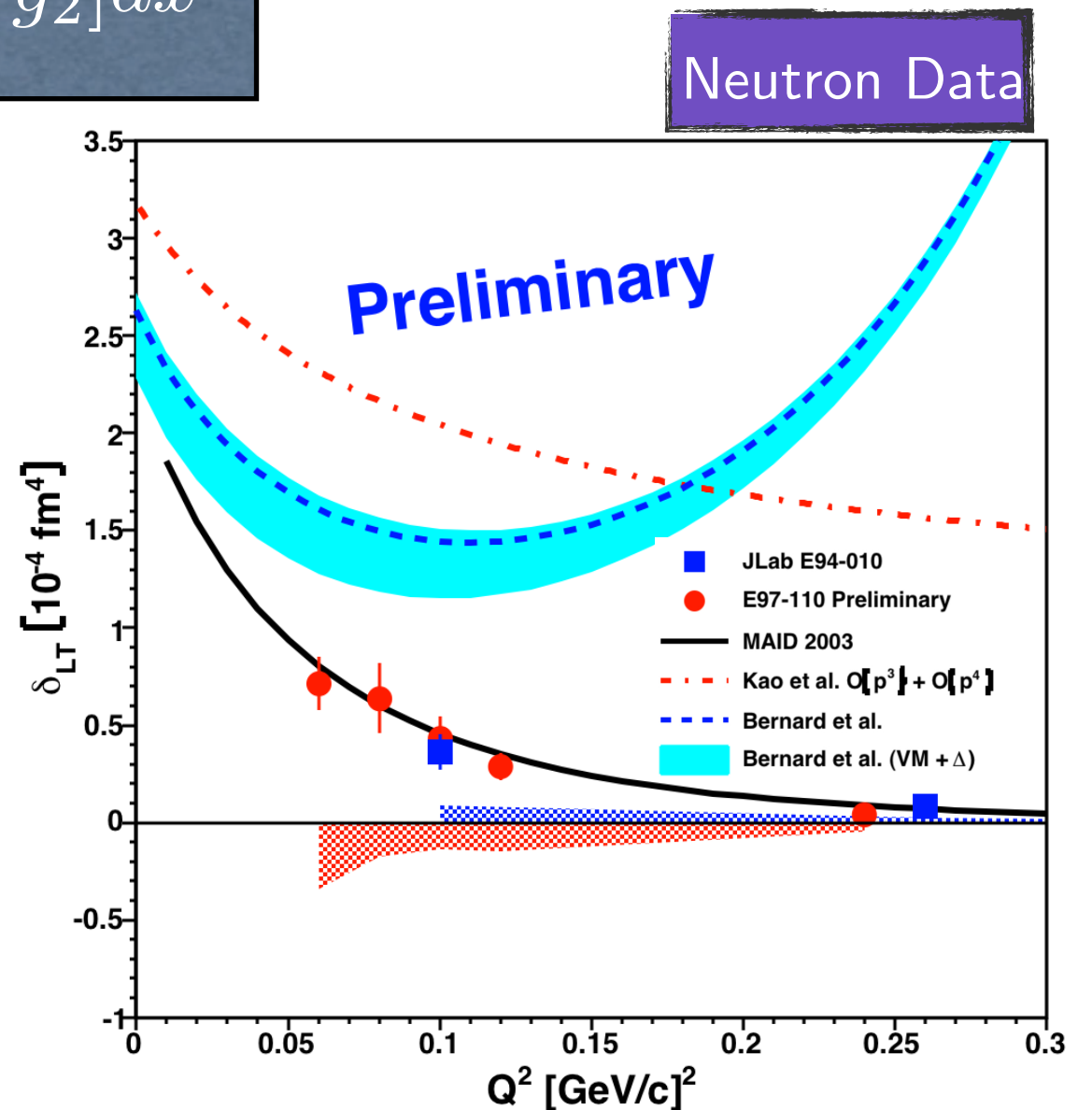


Particle Data Group (2010)

# Spin LT Polarizability

$$\delta_{LT}(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 [g_1 + g_2] dx$$

- Can be calculated via  $\chi$ PT
- Neutron data shows some deviations for calculated polarizabilities
- No proton data yet!



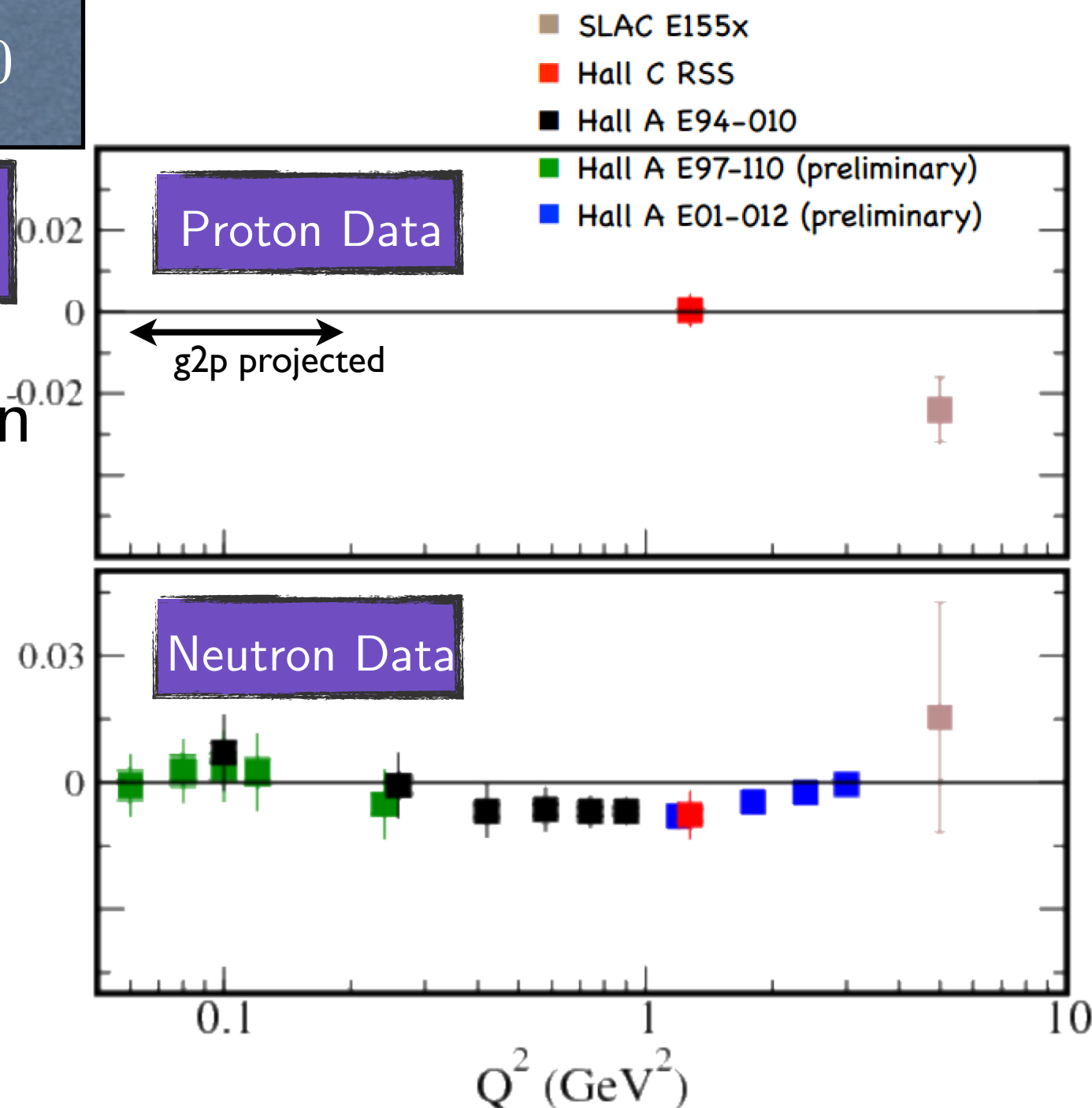
plot courtesy of V. Sulkosky

# The B.C. Sum Rule

$$\Gamma_2(Q^2) = \int_0^1 g_2(x, Q^2) dx = 0$$

H. Burkhardt and W.N. Cottingham  
Annals. Phys., 56 453 (1970)

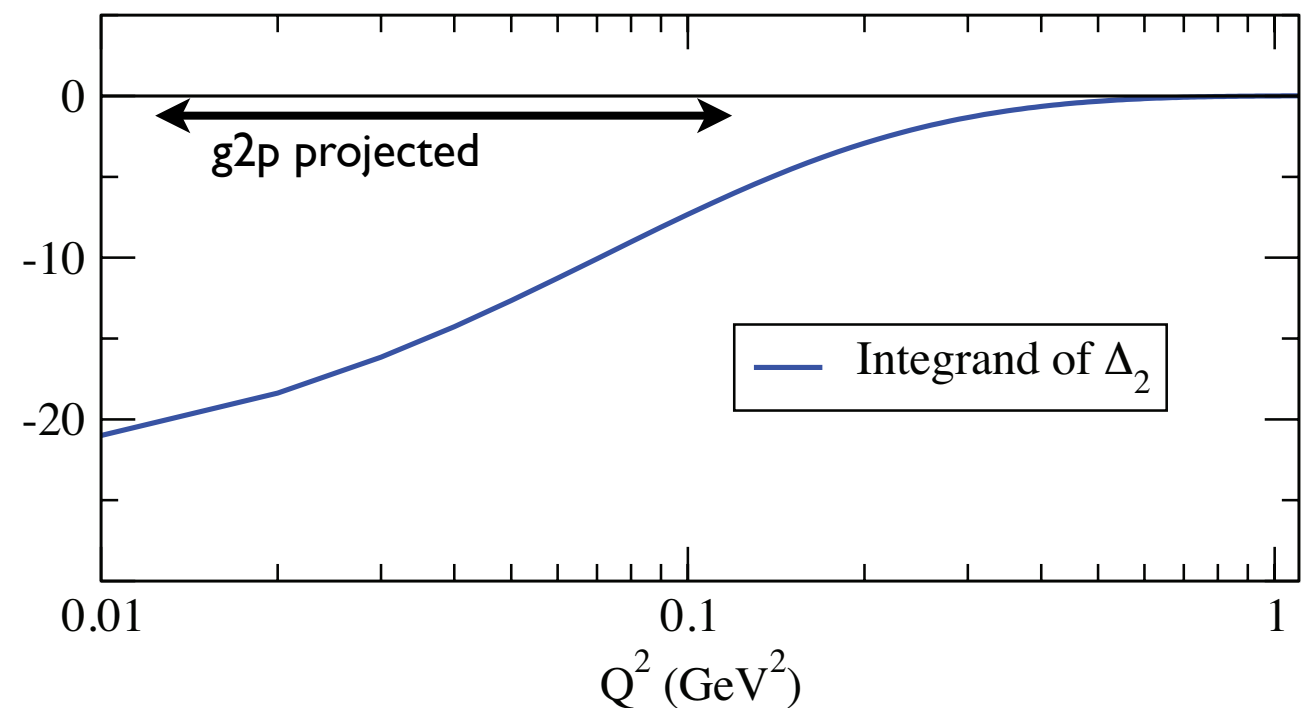
- Sum rule satisfied within errors for neutron
- Inconsistency seen in proton data
- Mostly unmeasured for proton



# Finite Size Effects

## Hydrogen Hyperfine Splitting

- $\Delta E = 1420.4057517667(9)\text{MHz}$   
 $= (1 + \delta)E_F$   
 $\delta = (\delta_{\text{QED}} + \delta_R + \delta_{\text{small}}) + \Delta_S$
- Structure correction has largest uncertainty to theoretical calculation



- $\Delta_S = \Delta_Z + \Delta_{pol}$ 
  - $\Delta_{pol} = \frac{\alpha m_e}{\pi g_p m_p} (\Delta_1 + \Delta_2)$

Dominated by low  $Q^2$   $g_2$

# Finite Size Effects

## Proton Charge Radius

- 2 ways to measure:
  - Energy splitting of  $2S_{1/2} - 2P_{1/2}$  level (Lamb shift)
    - $\Delta E = 209.9779(49) - 5.2262r_p^2 + 0.0347r_p^3$  meV
  - Scattering experiment
- Two results do not match
- Main uncertainties are from proton polarizability terms
  - Related to integral of spin structure functions

Lamb Shift

$$\langle R_p \rangle = 0.84182 \pm 0.00067 \text{ fm}$$

$$\langle R_p \rangle = 0.87680 \pm 0.0069 \text{ fm}$$

Scattering

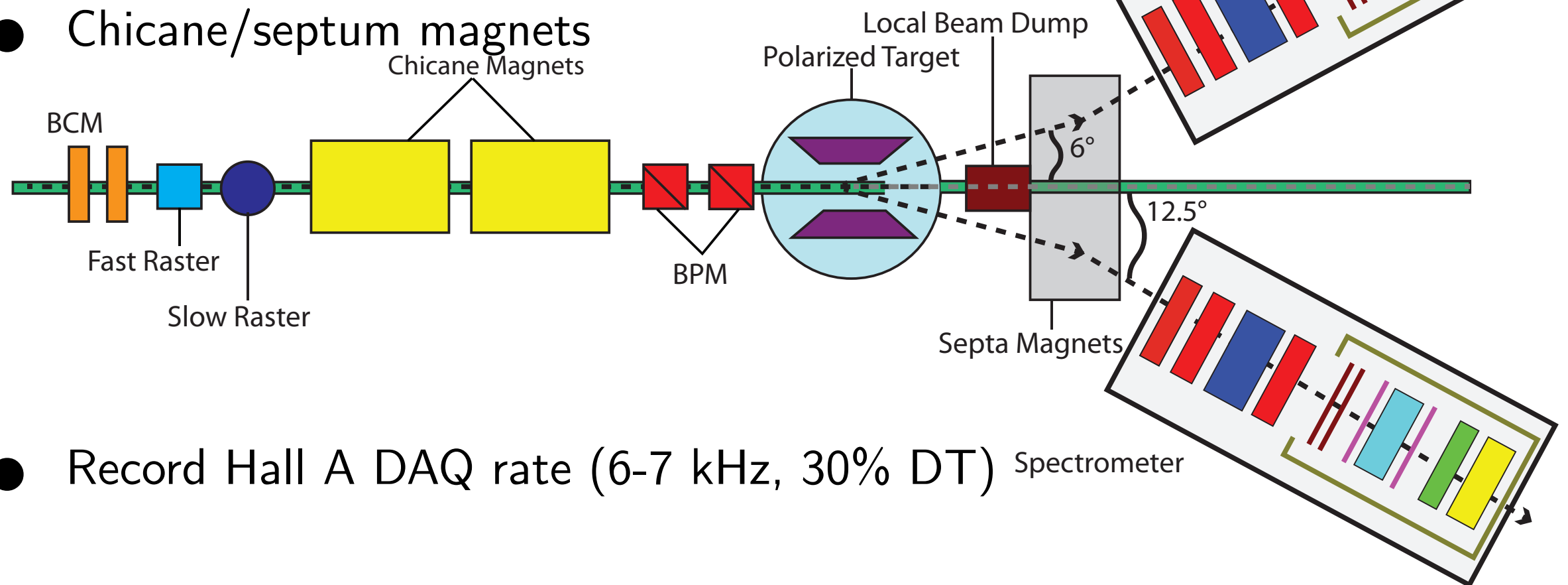
R. Pohl et al, Nature, 466(2010)213

# Experimental Set Up

JLab Hall A

- Large scale installation in Hall A
- Transverse polarized NH<sub>3</sub> target (2.5/5.0T field)
- Low current ( $< 100$  nA) beamline diagnostics

- Chicane/septum magnets

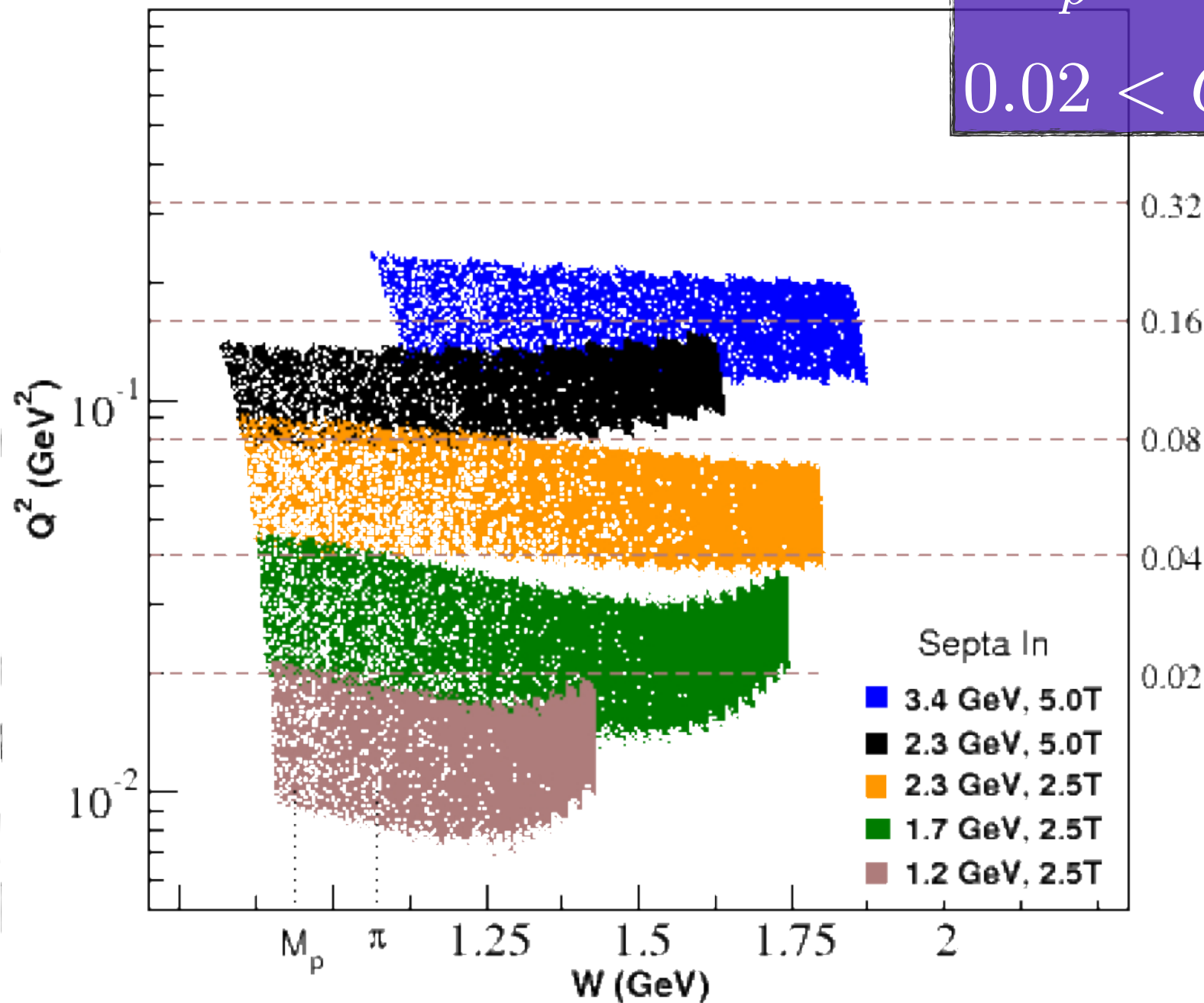


- Record Hall A DAQ rate (6-7 kHz, 30% DT)

# Kinematic Coverage

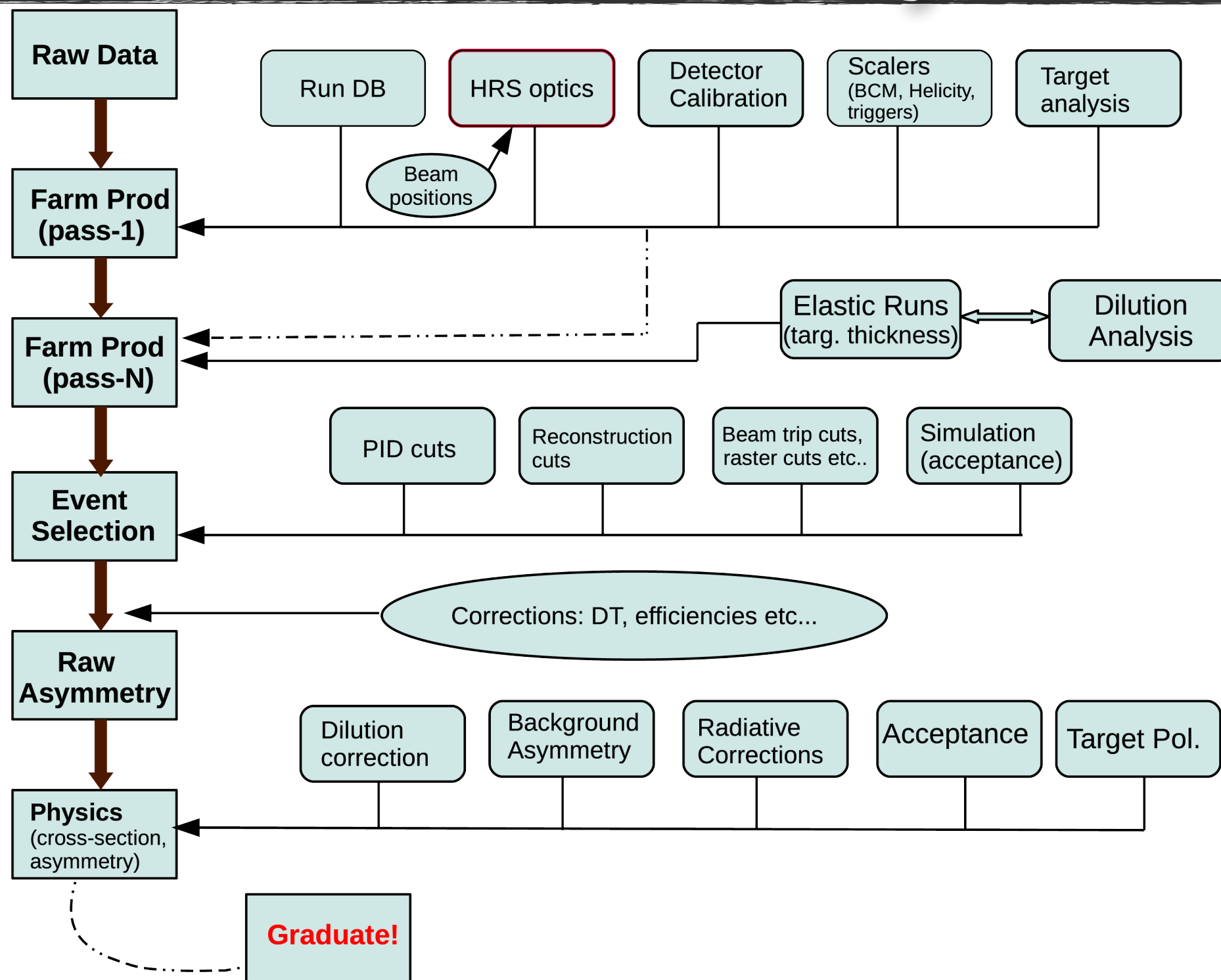
$$M_p < W < 2\text{GeV}$$

$$0.02 < Q^2 < 0.2\text{GeV}^2$$

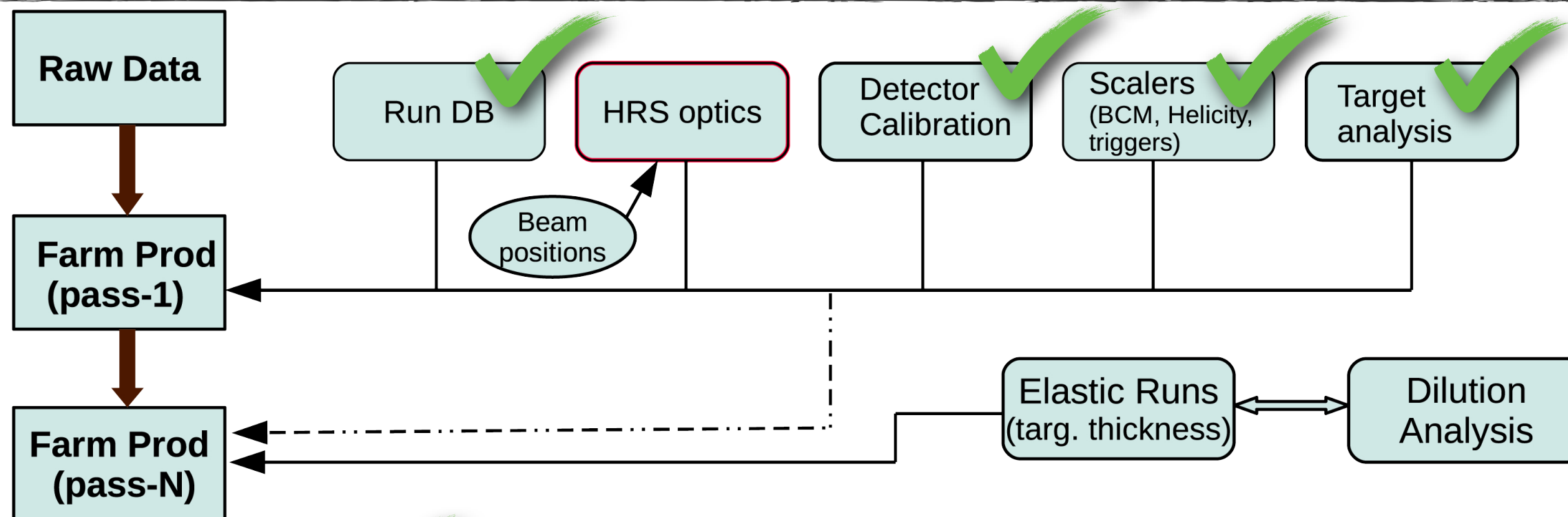


| Beam Energy (GeV) | Target Field (T) |
|-------------------|------------------|
| 2.254             | 2.5              |
| 1.706             | 2.5              |
| 1.158             | 2.5              |
| 2.254             | 5.0              |
| 3.352             | 5.0              |

# Status of Analysis



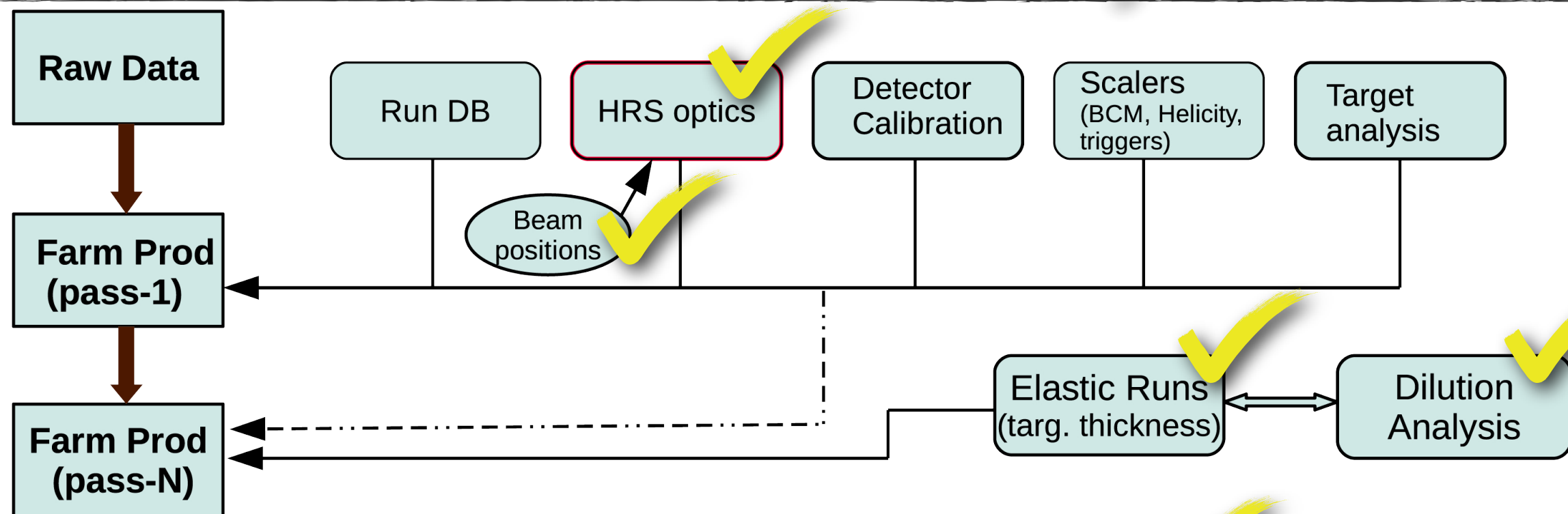
# Status of Analysis



Completed

- Run database
- HRS Optics w/o target field
- Detector Calibrations
- Scalers
- Target Polarization Analysis

# Status of Analysis



## Completed

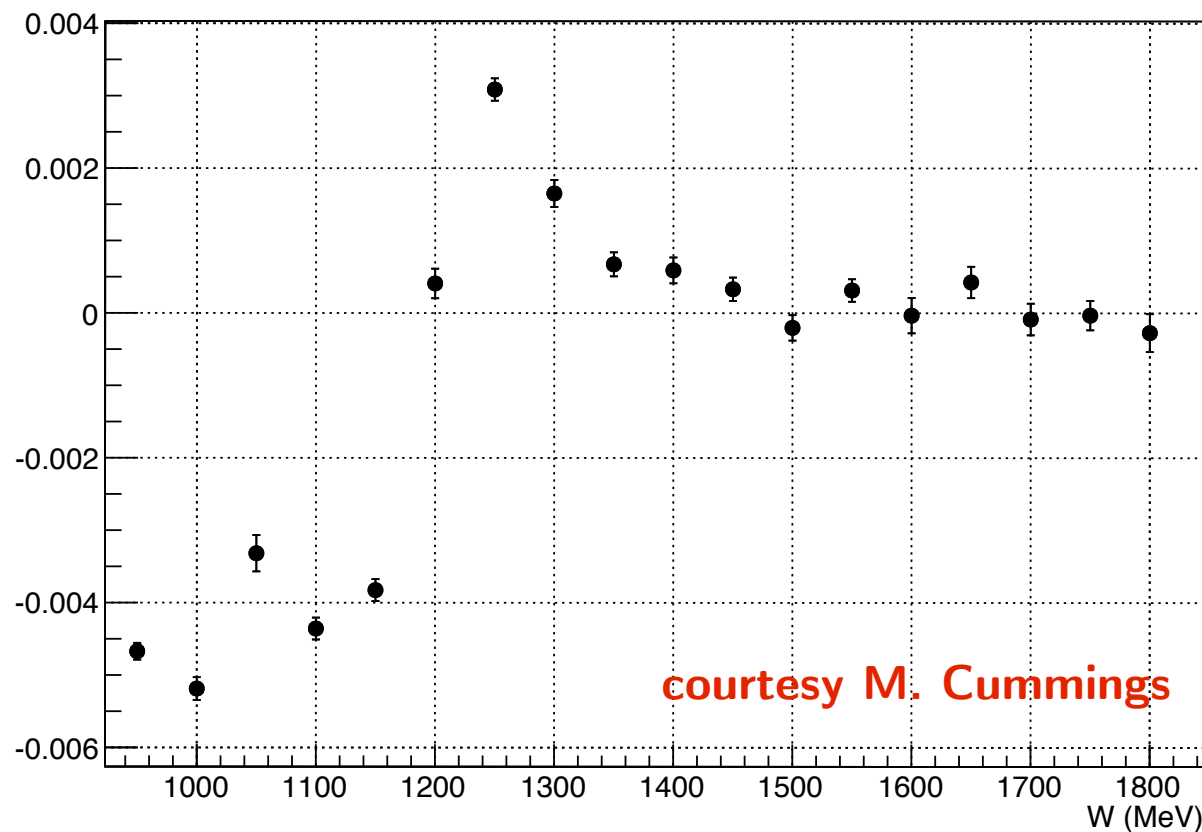
- Run database
- HRS Optics w/o target field
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- Target Polarization Analysis

## In Progress

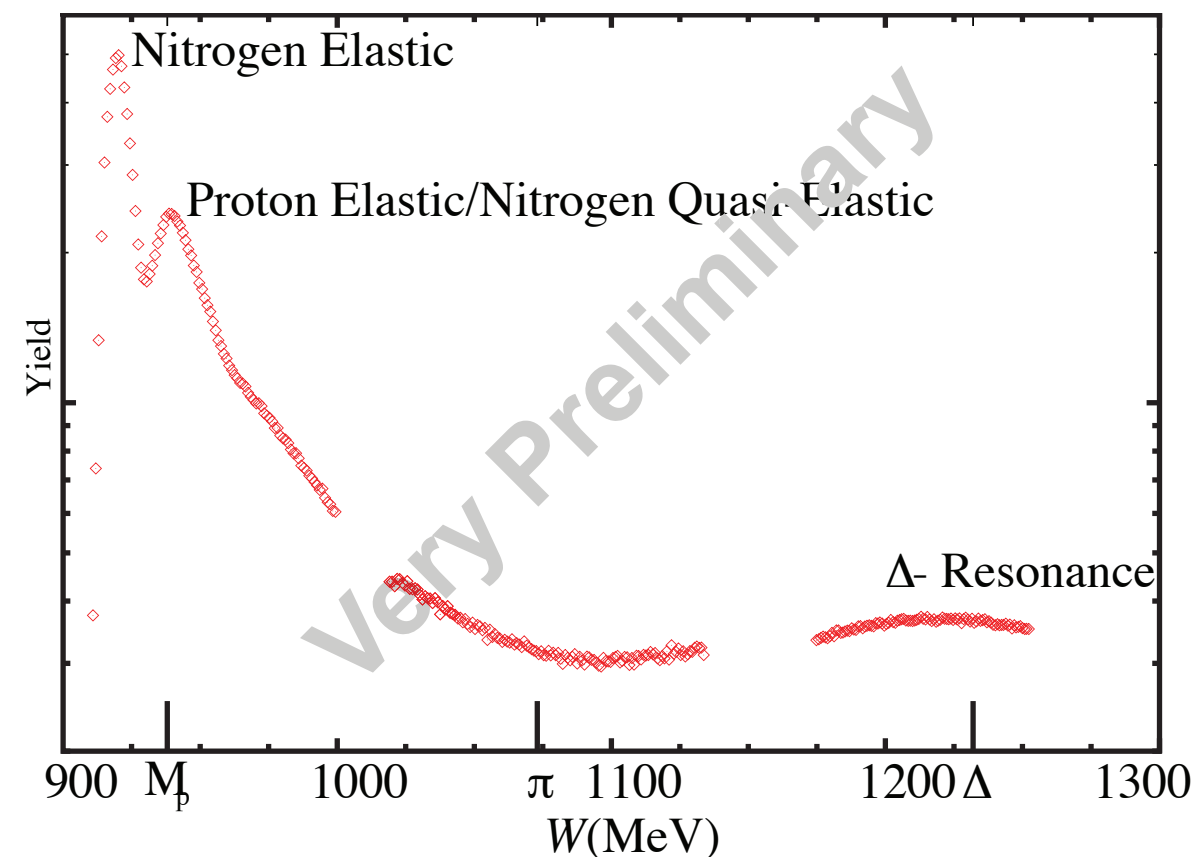
- Optics with target field
- BPM/raster calibrations
- Dilution Analysis
- Elastic Analysis
- Yield/Radiative Correction study

# Preliminary Offline Results

Asymmetry



Yield



$$A_{\perp} = \frac{\frac{d^2\sigma}{d\Omega dE'} (\downarrow \Rightarrow - \uparrow \Rightarrow)}{\frac{d^2\sigma}{d\Omega dE'} (\downarrow \Rightarrow + \uparrow \Rightarrow)}$$

$$\Delta\sigma_{\perp} = \frac{d^2\sigma}{d\Omega dE'} (\downarrow \Rightarrow - \uparrow \Rightarrow) = 2 \cdot A_{\perp} \sigma_{\perp}$$

Will measure asymmetry/cross section

# Summary

- The g2p experiment ran in spring 2012 and took data covering  $M_p < W < 2\text{GeV}$  and  $0.02 < Q^2 < 0.20\text{GeV}^2$
- Will provide a precision measurement of  $g_2^p$  in low  $Q^2$  region for the first time
- Results will shed light on several physics puzzles
  - Requires low  $Q^2$  data
- Data analysis is currently underway

# THANK YOU!

## E08-027 Analysis Team

### Spokespeople:

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### Post-Docs:

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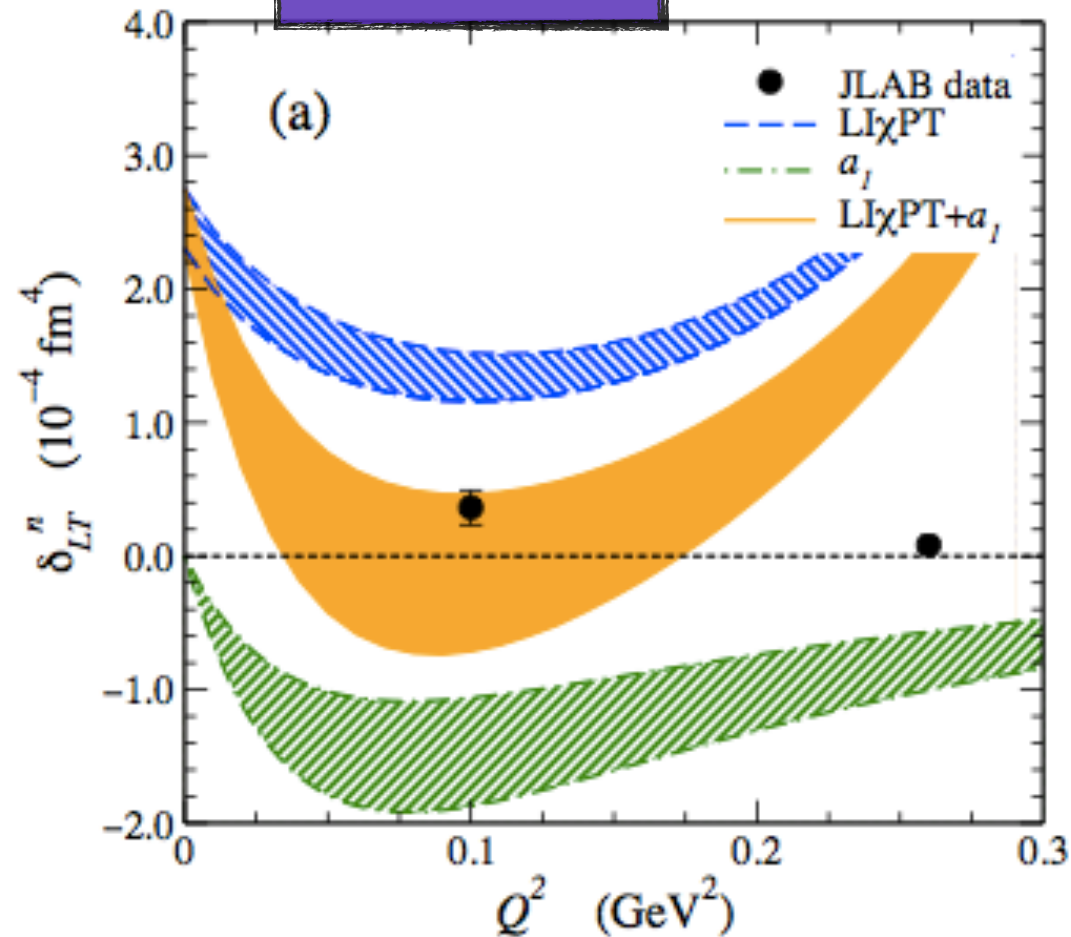
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Jie Liu  
Pengjia Zhu  
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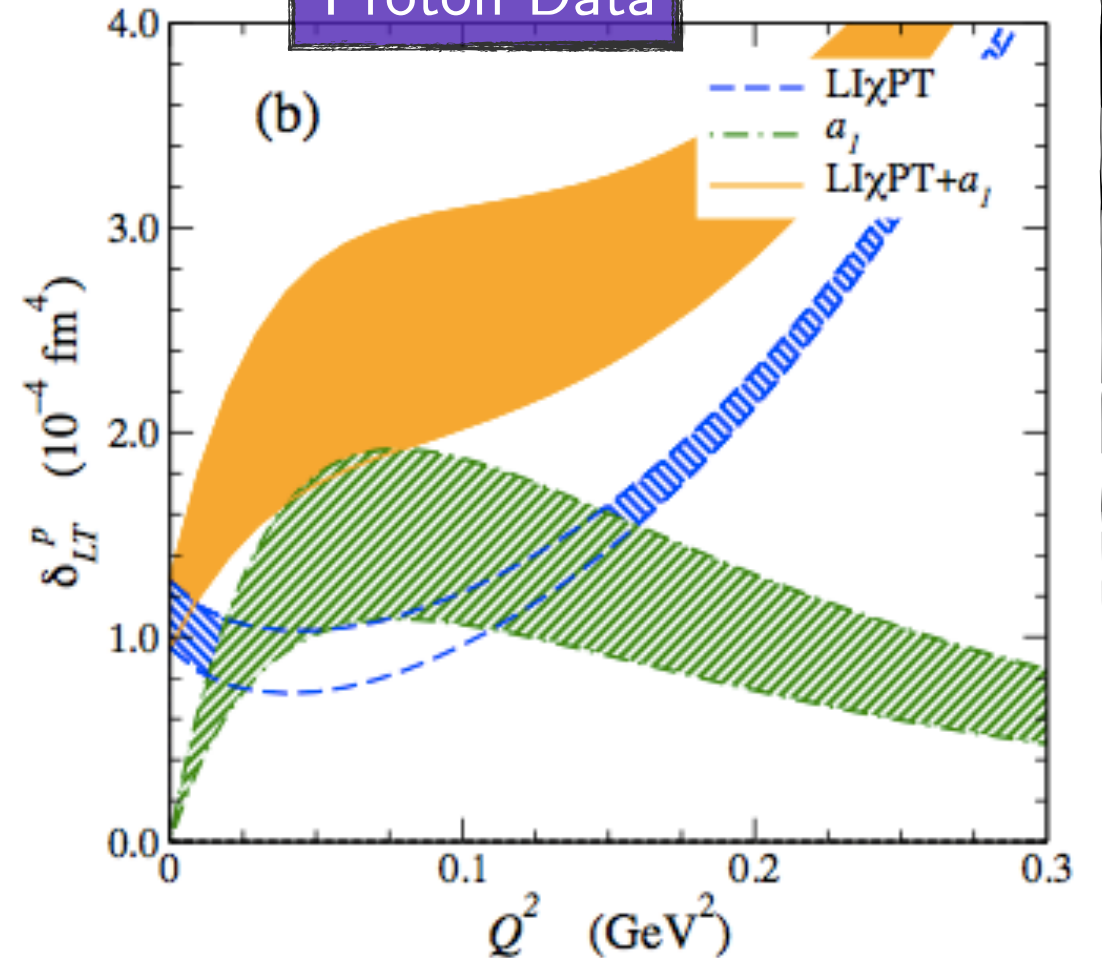
# Spin LT Polarizability

$$\delta_{LT}(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 [g_1 + g_2] dx$$

Neutron Data



Proton Data



Kochelev & Oh. arxiv:1103.4892 (2011)